

# CM0845 Logic

## Propositional Logic: Semantic Tableaux

Andrés Sicard-Ramírez

Universidad EAFIT

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## Remark

The reference for this section is Ben-Ari [2012, § 2.6].

## Semantics Tableaux

Theorem (Ben-Ari [2012], Theorem 2.67)

Let  $\varphi$  be a proposition and  $\mathfrak{T}$  be a completed tableau for  $\varphi$ . The proposition  $\varphi$  is unsatisfiable if and only if  $\mathfrak{T}$  is closed.

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### Example

Prove that  $\models (\varphi \wedge \psi \rightarrow \sigma) \rightarrow ((\varphi \rightarrow \sigma) \vee (\psi \rightarrow \sigma))$  using semantic tableaux [Ben-Ari 2012, Exercise 2.9, p. 46].

## References



- Ben-Ari, Mordechai [1993] (2012). Mathematical Logic for Computer Science. 3rd ed. Springer (cit. on pp. 2–4).