CM0081 Formal Languages and Automata Introduction to Haskell

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Features/Advantages

- Purely functional (verification)
- Statically typed (type-safe and maintainability)
- Lazy evaluation (unbounded data structures and performance)
- Garbage collected memory (no need for pointers)

Functions

Example (function application) Factorial function.

fac n = product [1..n]

Note: We use 'f n' instead of 'f(n)' for function application.

Types

Question

Is the fac function correct?

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Example

import Numeric.Natural

```
fac :: Natural -> Natural
fac n = product [1..n]
```

By writing down the type of the function we could avoid run-time errors.

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Other implementations for the factorial

Google for 'The evolution of a $\operatorname{Haskell}$ programmer'.

Curryfication

Example

Whiteboard.

Inductive definition

 $\operatorname{HASKELL}$ has built-in syntax for lists, where a list is either:

- the empty list, written [], or
- a first element x and a list xs, written (x : xs).

Example (pattern matching on lists)

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length [] = 0
length (x : xs) = 1 + length xs

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length [] = 0
length (x : xs) = 1 + length xs
```

Question

Can we avoid the boilerplate lstlisting? Yes!

Parametric Polymorphism

Example (basic functions from the @Data.List@ library)

(i) Returns the length of a finite list as an Int.

length :: [a] -> Int

(ii) Append two lists.

(++) :: [a] -> [a] -> [a]

(iii) Extract the first element of a list, which must be non-empty.

head :: [a] -> a

Parametric Polymorphism

Example (basic functions from the @Data.List@ library)

(i) Extract the last element of a list, which must be finite and non-empty.

last :: [a] -> a

(ii) Extract the elements after the head of a list, which must be non-empty.

tail :: [a] -> [a]

(iii) Return all the elements of a list except the last one. The list must be non-empty.

init :: [a] -> [a]

(iv) Test whether a list is empty.

null :: [a] -> Bool

Description

Nothing is evaluated until necessary.

Example

Infinite (unbounded) list.

ones :: [Int]
ones = 1 : ones

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Question

Which is the value of take 5 ones? [1,1,1,1,1]

Example (also in other programming languages)

Non-terminating function.

foo :: Int -> Bool
foo n = foo (n + 1)

Boolean disjunction.

bar :: Int -> Bool
bar n = True || foo n

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Question

Which is the value of bar 10? True

Example

(From stackoverflow.com/questions/30688558/)

```
dh :: Int -> Int -> (Int, Int)
dh d q = (2^d, q^d)
a, b :: (Int, Int)
a = dh 2 (fst b)
b = dh 3 (fst a)
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Question

Which is the value of a? (4,64)

Higher-Order Functions

Description

Functions are first-class citizen.

The expression map f xs is the list obtained by applying f to each element of xs:

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The function map can defined by

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Which is the value of map (+1) [1..5]? [2,3,4,5,6]

The function foldr applied to a binary operator, a starting value (typically the right-identity of the operator), and a list, reduces the list using the binary operator, from right to left:

foldr f z [x1, x2, ..., xn] = x1 `f` (x2 `f` ... (xn `f` z)...)

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The function foldl applied to a binary operator, a starting value (typically the left-identity of the operator), and a list, reduces the list using the binary operator, from left to right:

foldl f z [x1, x2, ..., xn] = (...((z `f` x1) `f` x2) `f`...) `f` xn

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Example

data Bool = True | False

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Functions by pattern matching

(||) :: Bool -> Bool -> Bool
True || _ = True
False || x = x

Example (recursive data type)

data Nat = Zero | Succ Nat

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Structural recursive function by pattern matching

(+) :: Nat -> Nat -> Nat Zero + n = n (Succ m) + n = Succ (m + n)

Example (polymorphic data type)

data	List a	a = Nil	Cons a (List a)
data	[] a	= []	a : [a]

The Real World

HASKELL in Industry (www.haskell.org/haskellwiki/Haskell_in_industry).
 Applications (www.haskell.org/haskellwiki/Libraries and tools).

- Homepage: www.haskell.org
- GHC: The Glorious Glasgow Haskell Compilation System
- ▶ GHCI: Interactive interpreter
- Toolchain: www.haskell.org/downloads
 - ▶ For installing GHC we suggest to use GHCUP.
 - For installing libraries and compiling programs you can use STACK or CABAL-INSTALL.
- Hackage: The HASKELL package repository
- Community: www.haskell.org/community/



Some Books

Bird, R. [2015]. Thinking Functionally with Haskell. Cambridge University Press.

- Hutton, G. [2007] [2016]. Programming in Haskell. 2nd ed. Cambridge University Press.
- Lipovača, M. [2011]. Learn You a Haskell for Great Good! No Starch Press.
- O'Sullivan, B., Goerzen, J. and Stewart, D. [2008]. Real World Haskell. O'Really Media, Inc.

A paper

Claessen, Koen and Hughes, John [2000]. QuickCheck: A Lightweight Tool for Random Testing of Haskell Programs. ICFP'00. DOI: https://doi.org/10.1145/357766.351266.

[†]See www.sigplan.org/Awards/ICFP/.

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Most Influential ICFP Paper Award 2010[†]

'The techniques described in the paper have spawned a significant body of follow-on work in test case generation. They have also been adapted to other languages ...'

[†]See www.sigplan.org/Awards/ICFP/.

Bonus Slides: Testing with $\operatorname{QUICK}C\operatorname{HECK}$

An open source library

QUICKCHECK on Hackage.[†]

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Adaptations

QUICKCHECK has been ported to various languages (Wikipedia 2024-02-02).

С	C#	C++	CHICKEN	Clojure
Common Lisp	Coq	D	Elm	Elixir
Erlang	$\mathrm{F}\#$	Factor	Go	Io
JAVA	JAVASCRIPT	Julia	Logtalk	LUA
MATHEMATICA	Objective-C	OCAML	\mathbf{Perl}	Prolog
PHP	Pony	Python	\mathbf{R}	Racket
Ruby	RUST	SCALA	Scheme	SMALLTALK
Standard ML	\mathbf{SWIFT}	TypeScript	VB.NET	VHILEY

Bonus Slides: Testing with QUICKCHECK

False positive

The program works properly but the test pointed out a fail:

- There is a bug elsewhere.
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False negative

There is a bug in the program but the test passed.

Recall Dijkstra's 1969 famous quote:

'Testing shows the presence, not the absence of bugs.'

Bonus Slides: Testing with $\operatorname{QUICKCHECK}$

Example

See demo.